Math 1050 - Solving Systems A5.1	Name
1. Solve by substitution: 2x + y = 7 x + 2y = 2	2. Solve by elimination: 4x - 3y = 11 8x + 4y = 12
3. Solve the system Graphically: $2x - 3y = 12$ $-x + \frac{3}{2}y = 4$	4. Solve the system: $3x + 2y = 0$ $-x - 2y = 8$
5. Solve the system: 4x-3y = 28 $9x-y = -6$	6. Solve the system: 0.2x - 0.2y = -1.8 -0.3x + 0.5y = 3.3
7. Solve the system: $-3x + 5y = 2$ $9x - 15y = 6$	8. Solve the system: 2x - 3y = -8 $14x - 21y = 3$

9.	Solve	the	system:
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$$\frac{1}{2}x + \frac{3}{5}y = 3$$

$$\frac{5}{3}x + 2y = 10$$

10. A man has 14 coins in his pocket all of which are dimes and quarters. If the total value of his change is \$2.75, how many dimes and how many quarters does he have?

- 11. A fruit stand sells 2 varieties of strawberries: standard and deluxe. A box of deluxe strawberries sells for \$7, and a box of deluxe sells for \$10. In one day the stand sells 135 boxes of strawberries for a total of \$1110. How many boxes of each type were sold?
- 12. Pop's Cycle Shop sells bicycles and tricycles. The number of bicycles is 1 less than 4 times the number of tricycles. All the bicycles and tricycles together have a total of 174 wheels. How many bicycles are there?

13. Suppose you have a job delivering packages. Assume that in both jobs you are working an 8 hour shift, and you work 20 days a month. The table below shows how much you currently earn in a month. You discover that a competitor pays employees \$2 per **hour** plus \$.35 per delivery.

CURRENT JOB:

deliveries made	Amount earned
5	\$1020
95	\$1020
170	\$1020
250	\$1020

14. Using the info at the left, find how many deliveries you would have to make to earn the same as you currently make.

How many deliveries is that a week?

How many deliveries is that a day?

How many deliveries in an hour?

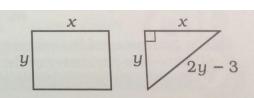
Which job would you choose? WHY? Write AT LEAST 2 FULL SENTENCES!

Equation for your current job:

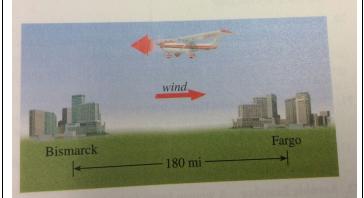
Equation for the competitor.

15.

The perimeter of the rectangle at right is 42 cm. The perimeter of the triangle is 36 cm. Find the values of x and y.



3. Airplane Speed A man flies a small airplane from Fargo to Bismarck, North Dakota—a distance of 180 mi. Because he is flying into a head wind, the trip takes him 2 hours. On the way back, the wind is still blowing at the same speed, so the return trip takes only 1 h 12 min. What is his speed in still air, and how fast is the wind blowing?



17. A biologist has 2 brine solutions, one containing 5% salt and another containing 20% salt. How many milliliters of each solutions should she mix to obtain 1L of a solutions containing 14% salt?

18.

4. Without using a graphing calculator, match each of the following functions to the graphs below. Give reasons for your choices.

$$f(x) = x^3 - 8x$$

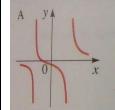
$$f(x) = x^3 - 8x$$
 $g(x) = -x^4 + 8x^2$ $r(x) = \frac{2x + 3}{x^2 - 9}$

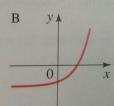
$$f(x) = \frac{2x+3}{x^2-9}$$

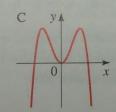
$$s(x) = \frac{2x-3}{x^2+9}$$
 $h(x) = 2^x - 5$ $k(x) = 2^{-x} + 3$

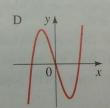
$$h(x) = 2^x - 5$$

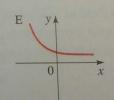
$$k(x) = 2^{-x} + 3$$

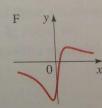












- 3. Let f be the quadratic function $f(x) = -2x^2 + 8x + 5$.
 - (a) Express f in standard form.
 - (b) Find the maximum or minimum value of f.
 - (c) Sketch the graph of f.
 - (d) Find the interval on which f is increasing and the interval on which f is decreasing.
 - (e) How is the graph of $g(x) = -2x^2 + 8x + 10$ obtained from the graph of f?
 - (f) How is the graph of $h(x) = -2(x+3)^2 + 8(x+3) + 5$ obtained from the graph of f?

9. Sketch graphs of the following functions on the same coordinate plane.

(a)
$$f(x) = 2 - e^x$$

(b)
$$g(x) = \ln(x+1)$$

- 10. (a) Find the exact value of $\log_3 16 2 \log_3 36$.
 - (b) Use the Laws of Logarithms to expand the expression

$$\log\left(\frac{x^5\sqrt{x-1}}{2x-3}\right)$$

11. Solve the equations.

(a)
$$\log_2 x + \log_2(x - 2) = 3$$

(b)
$$2e^{3x} - 11e^{2x} + 10e^x + 8 = 0$$
 [Hint: Compare to the polynomial in Problem 5.]

- 12. A sum of \$25,000 is deposited into an account paying 5.4% interest per year, compounded daily.
 - (a) What will the amount in the account be after 3 years?
 - (b) When will the account have grown to \$35,000?
 - (c) How long will it take for the initial deposit to double?
- 13. After a shipwreck, 120 rats manage to swim from the wreckage to a deserted island. The rat population on the island grows exponentially, and after 15 months there are 280 rats on the island.
 - (a) Find a function that models the population t months after the arrival of the rats.
 - (b) What will the population be 3 years after the shipwreck?
 - (c) When will the population reach 2000?